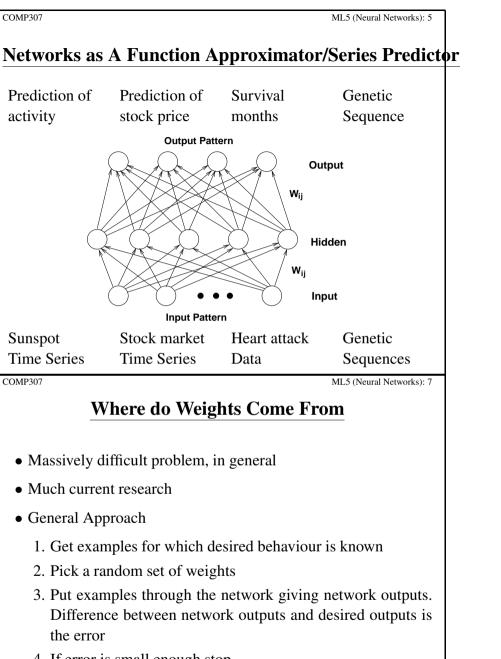
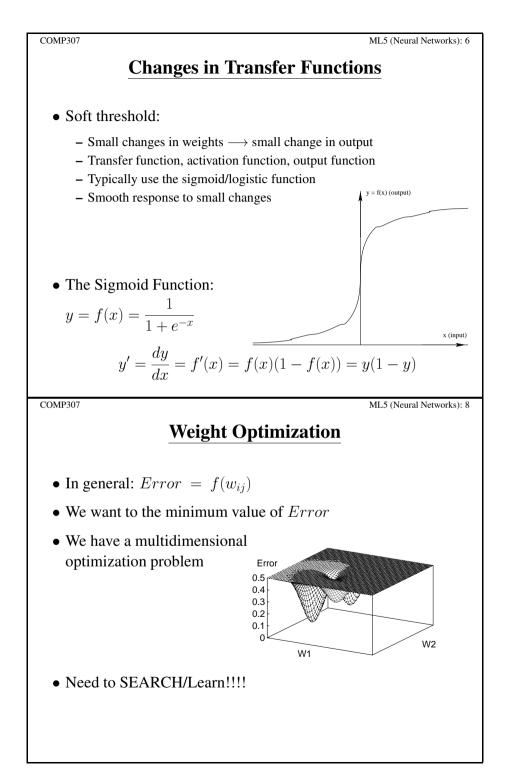
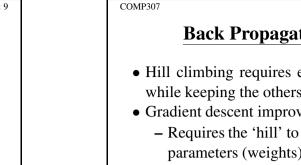
VICTORIA UNIVERSITY OF WELLINGTON	COMP307			ML5 (Neural Networks): 2
Te Whare Wananga o te Upoko o te Ika a Maui	Outline			
School of Engineering and Computer Science	• From perceptron to neural networks			
	• Network architecture			
COMP 307 — Lecture 08	• Back (error) propagation learning			
Machine Learning 5 Neural Networks and Back Propagation	<ul> <li>Gradient descent search</li> <li>Relationship between the weight change and the error, outputs</li> <li>Feed forward pass</li> <li>Back propagation pass</li> </ul>			
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COMP307 ML5 (Neural Networks): 3	COMP307			ML5 (Neural Networks): 4
Multilayer Perceptron (Neural Networks)	Feed Forv	vard Network	<u>ks as A Patter</u>	n Classifier
<ul> <li>Change one or two layers of nodes to three or more layers</li> <li>Multilayer perceptron (MLP)</li> <li>Feed forward neural networks</li> <li>Standard feed forward networks: nodes in neighbouring layers are fully connected</li> <li>Imput fielden fie</li></ul>	Digits in Postcode	Speech Recognition Output Pa	W <sub>ij</sub> W <sub>ij</sub>	Weather Prediction Output Hidden
– Output layer: output patterns/class labels	Picture of an	Speech	Sonar	Weather
– Hidden layer(s): high level features	Envelope	Waveform	Signal	Data



- 4. If error is small enough stop
- 5. Adjust current weights to make error smaller
- 6. Go to 3

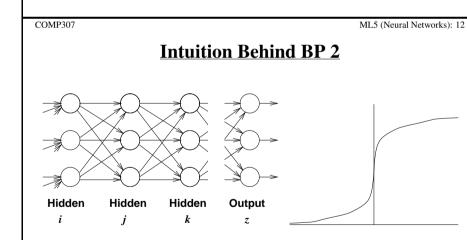


## ML5 (Neural Networks): 9



## **Back Propagation: Gradient Descent**

- Hill climbing requires evaluating the effect of one parameter while keeping the others constant
- Gradient descent improvement
  - Requires the 'hill' to be a smooth/continuous function of the parameters (weights)
  - Vary all weights simultaneously in proportion to how much good is done by individual changes
  - A move in the direction of the (steepest) gradient
- Back Propagation procedure
  - Relatively efficient procedure for computing how much performance (error reduction) improves with a weight change
  - Computes changes to final layer of weights first
  - Computes changes to next to last layer....initial layer
  - Requires a smooth transfer function

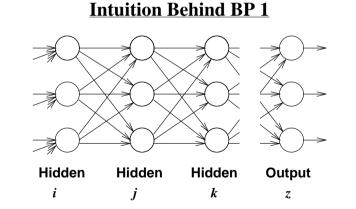


- A change in input to node *j* results in a change to output that depends on the *slope* of transfer function
- Change in input has maximum effect where the slope is steepest
- Slope of sigmoid/logistic is given by o(1 o)
- Thus  $\Delta w_{i \to j} \propto o_i (1 o_i)$

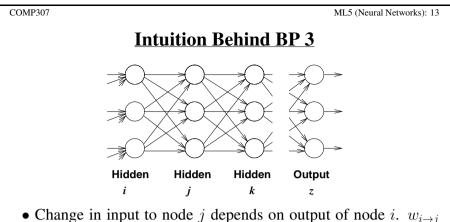
- **Network Training: Back Error Propagation**
- Input Units: Real numbers, usually scaled to be in [0,1]
- Hidden units: Activation  $\in [0, 1]$
- Output Units: Activation  $\in [0, 1]$
- Usually in fully connected layers, but this is not necessary.
- Transfer function: Logistic
- Units evaluated in serial/synchronous order
- Learning rule: *Generalized delta rule*
- Error of an output unit  $d_z o_z$
- Error of a pattern  $\sum_{z} (d_z o_z)^2$
- Total error of all training patterns
  - Total Sum Squared Error:  $TSS = \frac{1}{2} \sum_{patterns} \sum_{z} (d_z o_z)^2$
  - Root Mean Square Error (RMSE)  $\sqrt{2TSS/(numpat.numout)}$

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ML5 (Neural Networks): 11



- How big a change should we make to weight  $w_{i \rightarrow j}$ ?
- Make a big change if it will result in a big improvement in error
- If a change to  $w_{i \rightarrow j}$  will have little effect on on error, make it small



- Change in input to node j depends on output of node i. w<sub>i→j</sub> should change substantially if o<sub>i</sub> is high. Thus ∆w<sub>i→j</sub> ∝ o<sub>i</sub>
- Let β be a factor which measures how beneficial the change is (in terms of lower error). Node j is connected to nodes in next (kth) layer. A change in o<sub>j</sub> will be a benefit to each one. So

Hidden:  $\beta_j = \sum_k w_{j \to k} o_k (1 - o_k) \beta_k$ 

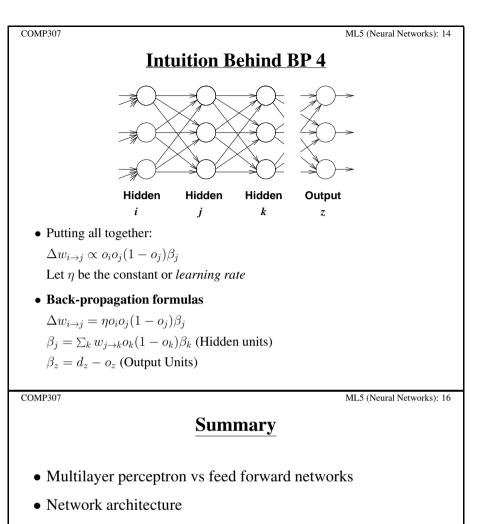
Output: 
$$\beta_z = d_z - o_z$$
 and  $\Delta \mathbf{w}_{\mathbf{i} \to \mathbf{j}} \propto \beta_{\mathbf{j}}$ 

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ML5 (Neural Networks): 15

## **BP** Algorithm

- Let  $\eta$  be the learning rate.
- Set all weights, including biases to small random values.
- Until total error (TSS or RMSE) is small enough do
  - For each input vector
    - \* Feed forward pass to get outputs
    - \* Compute  $\beta$  for output nodes  $\beta_z = d_z o_z$
    - \* Compute  $\beta$  for hidden nodes, working from last layer to first layer  $\beta_j = \sum_k w_{j \to k} o_k (1 - o_k) \beta_k$
    - \* Compute and store weight changes for all weights  $\Delta w_{i \rightarrow j} = \eta o_i o_j (1 o_j) \beta_j$
  - Add up weight changes for all input vectors and change the weights



- NN applications
- Back (error) propagation learning
  - Gradient descent search
  - Relationship between the weight change and the error, outputs
  - Feed forward pass
  - Back propagation pass